

Investigation of Local Distortion Effects on X-Ray Absorption of Ferroelectric Perovskites from First Principles Simulations

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Experimental XAS Measurements:

Experimental XAS results were obtained on BaTiO₃ thin films (~10 nm thick) synthesized by reactive MBE deposited on (0.5 wt.%) Nb-doped (001)-oriented SrTiO₃ substrates. The detail of growth is discussed in detail in our previous work.¹ XAS experiments were performed at the XTIP² beamline 4-ID-E of the Advanced Photon Source and Center for Nanoscale Materials in Argonne National Laboratory. Polarization reversal was achieved by biasing sample with ± 10 V with an STM tip in tunneling mode for 10 minutes. O-K and Ti-L edges were probed by XAS spectra was achieved by changing the beam energy from 525 to 545 eV and 453.5 to 468.5 eV with a step size of 0.1 eV to probe, respectively.

First-Principles Computational XAS:

First-principles XAS simulations were performed on a 1x1x5 symmetric slab with ~15 Å of vacuum at each side. To model the BaTiO₃ thin film, we used a tetragonal (*P4mm*) unit cell with a lattice constant of $a=3.99$ Å and $c=4.03$ Å. Implementing periodic boundary conditions (PBC) on the slab geometry is critical to mimic the properties of an experimental thin film with broken symmetry along the z axis, while enabling the possibility of creating surface sites and local distortion effects. Moreover, limiting the supercell size to 1x1x5, with less than 30 atoms, makes tractable the computationally demanding, non-self-consistent electronic and BSE screening calculations. To represent the upward and downward polarization states and symmetry breaking across the slab model, the topmost layer was distorted as detailed in Table 1. The calculated local polarization (per unit cell), based on a berry-phase³ model for each of these distortions, is also listed.

Here upward distortion of Ti atoms within the oxygen octahedron toward the surface of slab model (vacuum) is denoted as P⁺, while a downward displacement toward the film is denoted as P⁻.

(i) *Many-body Δ SCF determinant approach:*

The results based on the many-body Δ SCF determinant formalism was simulated using MBXAS code.⁴ Ground state DFT calculations were performed with Quantum ESPRESSO.⁵ The generalized gradient approximation of Perdew, Burke, and Ernzerhof (PBE)⁶ was used to properly describe O-p and Ti-d orbitals of BaTiO₃. Supercell calculations were performed with $2 \times 2 \times 2$ k-point grids. The calculations used a 30 Ry kinetic energy and 300 Ry charge-density cutoff, with a gaussian broadening of 0.2 eV. The core-excited electronic structure and associated orbitals used in spectral line-shape calculations were computed within the full-core hole (FCH) approximation. The spectra for different materials and for different excited sites within the same material were aligned based on the position of the main edge of the element in the experimental dataset. The 1s core-excited O atom was simulated using a pseudo-potential with configuration of $1s^1 2s^2 2p^4$.

In many-body determinant Δ SCF approach is the equilibrated electron density in the presence of a core hole, while the initial state is taken as the ground state of the pristine system.⁴ The transition amplitude is approximated based on using the Kohn-Sham orbitals, based on the following equation:

$$\langle \psi_f | \varepsilon \cdot R | \psi_i \rangle = S \langle \psi_f | \varepsilon \cdot r | \psi_h \rangle$$

where ε stand for photon polarization, R is the many-body position operator, ψ_f is the unoccupied orbitals in the final state, and ψ_h is the core orbital in the initial state. S is a many-body overlap that reflects the excited-state response of the remaining electrons other than the photoexcited one.⁴

(ii) Hybrid GW/BSE Approach:

Computational XAS results were obtained based on BSE approach using OCEAN 2.9.7 (Obtaining Core Excitations from Ab initio electronic structure and NBSE) code.⁷ Ground state DFT calculations were obtained using Quantum ESPRESSO,⁵ with norm-conserving pseudopotentials from the pseudo-dojo distribution. A 2 x 2 x 2 k-point grid was used to solve the Kohn–Sham equations, and a total of ~1700 bands were used for the screening calculations. The final state is assumed to be a superposition of effective e-h pairs, whose matrix elements are calculated based on the following equation:

$$\langle \psi_f | \varepsilon \cdot R | \psi_i \rangle = \sum_c A_c^{f*} \langle \psi_c | \varepsilon \cdot r | \psi_h \rangle$$

where ψ_c are the initial-state orbitals and c iterates over empty orbitals only. The exciton amplitude

A_c^{f*} and energy E_f can be solved from the BSE method.⁴

Supplementary Tables:

Table S1. Values for local distortions associated with different extent of upward and downward polarization, noted as P1 and P2.

Polarization	Relative Distortion (d/c)	Absolute Distortion (\AA)	Berry Phase Polarization
P1	0.0215	0.087	18 $\mu\text{C}/\text{cm}^2$
P2	0.0430	0.174	32 $\mu\text{C}/\text{cm}^2$

Table S2. Values for relative peak ratios on O-K edge of the surfaces in upward and downward polarization based on experimental data and calculations with P1 and P2 polarization values.

<i>O-K Experiment</i>				
Peak	P+/P-	t_{2g} / e_g	P+	P-
t_{2g}	1.17		1.31	1.29
e_g	1.14			
<i>O-K ΔSCF (P1)</i>				
t_{2g}	1.05	t_{2g} / e_g	1.03	1.14
e_g	1.16			
<i>O-K ΔSCF (P2)</i>				
t_{2g}	1.09	t_{2g} / e_g	0.94	1.07
e_g	1.25			
<i>O-K BSE (P1)</i>				
t_{2g}	1.09	t_{2g} / e_g	1.90	1.73
e_g	0.99			
<i>O-K BSE (P2)</i>				
t_{2g}	1.22	t_{2g} / e_g	2.19	1.49
e_g	0.83			

Table S3. Values for relative peak ratios on O-K edge of the surfaces in upward and downward polarization based on experimental data and calculations with P1 and P2 polarization values.

<i>Ti-L Experiment</i>				
Peak	P+/P-		P+	P-
L3- t_{2g}	1.18	L3 t_{2g} / e_g	0.64	0.64
L3- e_g	1.17			
L2- t_{2g}	1.30	L2 t_{2g} / e_g	0.56	0.52
L2- e_g	1.21			
<i>Ti-L ΔSCF (P1)</i>				
L3- t_{2g}	1.12	L3 t_{2g} / e_g	1.93	1.86
L3- e_g	1.07			
L2- t_{2g}	N/A	L2 t_{2g} / e_g	N/A	N/A
L2- e_g	N/A			
<i>Ti-L ΔSCF (P2)</i>				
L3- t_{2g}	1.15	L3 t_{2g} / e_g	1.88	1.86
L3- e_g	1.14			
L2- t_{2g}	N/A	L2 t_{2g} / e_g	N/A	N/A
L2- e_g	N/A			
<i>Ti-L BSE (P1)</i>				
L3- t_{2g}	1.03	L3 t_{2g} / e_g	0.49	0.55
L3- e_g	1.11			
L2- t_{2g}	1.05	L2 t_{2g} / e_g	0.66	0.80
L2- e_g	1.09			
<i>Ti-L BSE (P2)</i>				
L3- t_{2g}	1.17	L3 t_{2g} / e_g	0.66	0.80
L3- e_g	1.13			
L2- t_{2g}	1.23	L2 t_{2g} / e_g	0.59	0.70
L2- e_g	1.09			

Supplementary Figures:

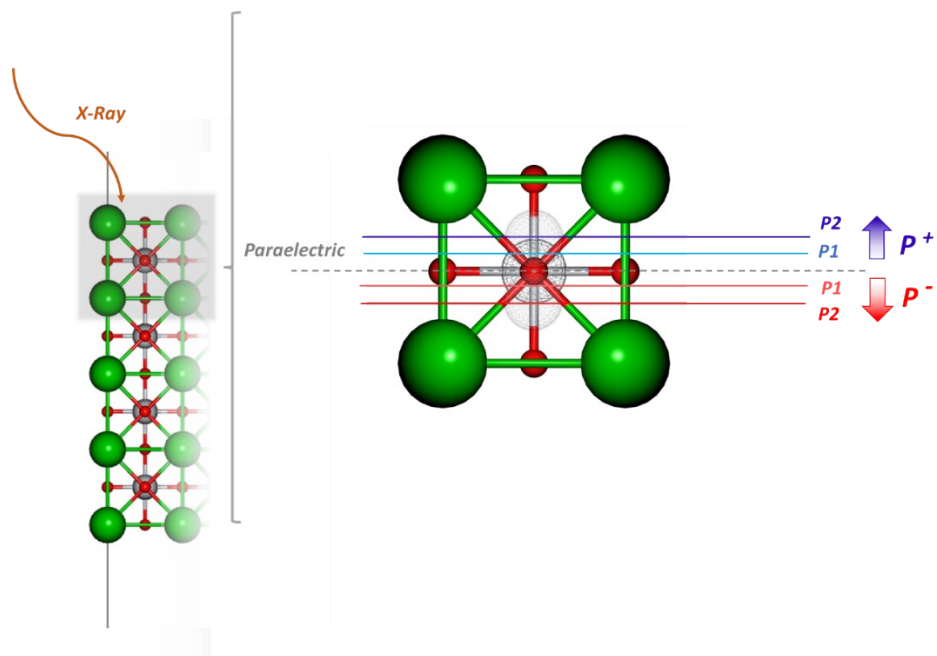


Figure S1. Schematic of the slabs used for XAS calculations, slab with different extent of upward and downward polarization, noted as P1 and P2.

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